

## Theorems

\* The Divergence theorem of Gauss:

This theorem states that if  $V$  is the volume bounded by a closed surface  $S$  and  $\vec{A}$  is a vector function of position with continuous derivatives, then

$$\iiint_V \nabla \cdot \underline{A} \, dV = \iint_S \underline{A} \cdot \hat{n} \, dS = \oiint_S \underline{A} \cdot d\underline{s}$$

where  $\hat{n}$  is the positive (outward drawn) normal to  $S$ .

\* Stoke's theorem: This theorem states that if  $S$  is open, two-sided surface bounded by a closed, non-intersecting curve  $C$  (simple closed curve) then if  $\vec{A}$  has continuous derivatives



$$\oint_C \underline{A} \cdot d\underline{r} = \iint_S (\nabla \times \underline{A}) \cdot \hat{n} \, dS = \iint_S (\nabla \times \underline{A}) \cdot d\underline{s}$$

where  $C$  is traversed in the positive direction.

\* Green's theorem in the plane: If  $R$  is a closed region in the  $xy$  plane bounded by a simple closed curve  $C$  and if  $M$  &  $N$  are continuous functions of  $x$  &  $y$  having continuous derivatives in  $R$ , then

$$\oint_C M dx + N dy = \iint_R \left( \frac{\partial N}{\partial x} - \frac{\partial M}{\partial y} \right) dx dy$$

where  $C$  is traversed in positive direction.

